

MAT3-119 Calculus of a Single Variable

Quiz 6 November 16, 2015

solution

name

You must either justify your answers and/or show your work. Don't approximate your answers unless directed to do so. Graphing calculators are allowed.

1. (6 pts.) Find the derivative of the following functions:

a.  $f(x) = x^4 2^x$

$$4x^3 2^x + x^4 \ln 2 2^x$$

b.  $g(x) = \sqrt{1-x^2}$

$$\frac{1}{2\sqrt{1-x^2}} \cdot -2x = \frac{-x}{\sqrt{1-x^2}}$$

c.  $\cos^2(x^3) = (\cos(x^3))^2$

$$y' = 2(\cos(x^3)) \cdot -\sin(x^3) \cdot 3x^2$$

2. (4 pts.) Use the quotient rule to derive the formula for the derivative of  $\tan x$ .

$$(\tan x)' = \left( \frac{\sin x}{\cos x} \right)' = \frac{\cos x \cdot \cos x - \sin x \cdot -\sin x}{(\cos x)^2}$$

$$= \frac{1}{(\cos x)^2} = \sec^2 x$$